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# *E–J* characteristics and *n*-values of a niobium–tin superconducting wire as a function of magnetic field, temperature and strain

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# Abstract

Systematic measurements have been made of the E-J characteristics of a Nb<sub>3</sub>Sn wire over four decades of electric field (0.1–1000  $\mu$ V m<sup>-1</sup>) and five decades of current density (10<sup>3</sup>–5 × 10<sup>8</sup> A m<sup>-2</sup>) as a function of magnetic field, temperature and strain. They were parameterised using the power law  $E = \alpha J^n$ . At low magnetic fields *n* tends to a constant saturation value, which decreases at high compressive and tensile strains and increases with increasing electric field. In the high magnetic-field range, *n* is independent of *E*-field and can be approximated by a strain and temperature scaling law of the form  $n(B, T, \varepsilon) = G(T)(B_{c2}^*(T, \varepsilon) - B)$ , where  $B_{c2}^*(T, \varepsilon)$  is an effective upper critical field.  $\mathbb{C}$  2002 Elsevier Science B.V. All rights reserved.

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# 1. Introduction

The electric field-current density (E-J) characteristics of a superconducting wire can be described by the power law  $E = \alpha J^n$ . The *n*-values provide important technological data for high *E* (fusion) and low *E* (NMR) magnet systems, and can be related to the microstructure of the wire and the transition from the flux-pinned to fluxflow state [1,2]. This paper presents detailed measurements of the *n*-value as a function of field, temperature and strain.

### 2. Experimental details

Measurements were made on a standard 0.81 mm diameter bronze-route Nb<sub>3</sub>Sn multifilamentary wire on a copper-beryllium alloy spring sample-holder using the Durham  $J_c(B, T, \varepsilon)$  probe [3]. The current (*I*) was slowly increased, and the voltage (*V*) across a section of the wire was measured using a nanovolt amplifier and digital voltmeter. In addition, AC resistance measurements were made to determine the upper critical field  $(B_{c2}(T, \varepsilon))$ .

The shunt resistance was measured at 20 K as a function of field, and a shunt current was subtracted from the total current. In addition, a linear thermal offset voltage (typically  $\sim 2 \text{ pV A}^{-1}$ ) was subtracted from the measured voltage. Finally, *E* 

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and J were calculated from the V–I data using the tap separation (20.3 mm) and the cross-sectional area of the wire  $(5.15 \times 10^{-7} \text{ m}^2)$ .

## 3. Results and discussion

Fig. 1 shows on a log-log scale a typical set of *E-J* characteristics at different fields measured at 0% applied strain at 12 K. The high-field data are almost completely straight over four decades of electric field. The *n*-values for the electric-field range 10–100  $\mu$ V m<sup>-1</sup> are plotted as a function of strain at 8 K in Fig. 2 and at 12 K in Fig. 3. At both temperatures, the *n*-values for a given field peak at  $\varepsilon = 0.33\%$ .

Fig. 4 shows *n* for the range 1–10  $\mu$ V m<sup>-1</sup> as a function of field at different strains at 12 K. Above  $B_{c2}$ , *n* is close to 1, corresponding to ohmic *E*–*J* characteristics. At high fields, below  $B_{c2}$ ,  $\partial n/\partial B$  is independent of magnetic field, electric field and strain. At low fields *n* approaches a saturation value ( $n_0$ ), which has a maximum at  $\varepsilon = 0.33\%$  and decreases for high compressive and tensile strains. Fig. 5 shows *n* for two different *E*-field ranges as a function of field at different strains at 8 K. For the higher *E*-field range (10–100  $\mu$ V m<sup>-1</sup>) the saturation of *n* occurs at a higher value and a lower magnetic field. The *n*-values for the ranges 0.1–1 and 100–1000  $\mu$ V m<sup>-1</sup> (not shown) have even lower



Fig. 1. A log-log plot of the electric field (*E*) versus engineering current density (*J*) for the wire at 12 K, at 0% applied strain and at half-integer magnetic fields between 3 and 15 T.



Fig. 2. The *n*-value for the electric-field range  $10-100 \,\mu\text{V}\,\text{m}^{-1}$  as a function of applied strain ( $\epsilon$ ) at 8 K and at integer magnetic fields between 2 and 15 T.



Fig. 3. The *n*-value for the range  $10-100 \ \mu V m^{-1}$  as a function of applied strain ( $\epsilon$ ) at 12 K and at half-integer magnetic fields between 0.5 and 4 T and integer fields between 4 and 12 T.

and even higher values of  $n_0$  respectively. At high fields *n* is independent of the *E*-field range, corresponding to power law *E*-*J* characteristics. The data at 4.2 and 12 K show similar features to the 8 K data.

An effective upper critical field  $(B_{c2}^*(T,\varepsilon))$  at 8 and 12 K can be obtained for strains above -1.11% by extrapolating the linear part of the n(B) curves to n = 0. These values are plotted in Fig. 6, along with AC resistivity measurements of  $B_{c2}$  defined at 5%, 50% and 95% of the normal state resistivity ( $\rho_n$ ). It can be seen that  $B_{c2}^* \approx B_{c2}^{0.5\rho_n}$ 



Fig. 4. The *n*-value for the range  $1-10 \ \mu V m^{-1}$  as a function of magnetic field (*B*) at different applied strains ( $\varepsilon$ ) at 12 K.



Fig. 5. The *n*-value for the range  $1-10 \ \mu V m^{-1}$  (closed symbols) and  $10-100 \ \mu V m^{-1}$  (open symbols) as a function of magnetic field (*B*) at different applied strains ( $\varepsilon$ ) at 8 K.

except near the peak (at  $\varepsilon = 0.33\%$ ). The n(B) data at 8 and 12 K have been replotted as a universal function of  $B - B_{c2}^*$  in Fig. 7. At fields above the saturation region the *n*-value can be approximated by

$$n(B,T,\varepsilon) = G(T)(B^*_{c2}(T,\varepsilon) - B), \tag{1}$$

where  $G = 2.75 \text{ T}^{-1}$  at 8 K and 1.95 T<sup>-1</sup> at 12 K.

It is proposed that in the high-field region the intrinsic properties of the wire determine n, while in the low-field region extrinsic properties cause n



Fig. 6. The upper critical field  $(B_{c2})$  as a function of applied strain ( $\varepsilon$ ) at 8 and 12 K.  $B_{c2}$  was determined at 5%, 50% and 95% of the normal state resistivity ( $\rho_n$ ), and also an effective value  $(B_{c2}^*)$  was determined from the *n*-value data.



Fig. 7. The *n*-value for the ranges 1–10 and 10–100  $\mu$ V m<sup>-1</sup> as a function of magnetic field (*B*) minus an effective upper critical field ( $B_{c2}^*$ ). The straight lines show the gradients (*-G*) of the linear parts of the data at 8 and 12 K.

to saturate in a way that depends on the strain state and the *E*-field range [1].

# 4. Conclusions

The E-J characteristics of a Nb<sub>3</sub>Sn wire were measured as a function of magnetic field, temperature and strain and parameterised using the power law  $E = \alpha J^n$ . Electric fields between 0.1  $\mu$ V m<sup>-1</sup> (2 nV) and 1000  $\mu$ V m<sup>-1</sup> (20  $\mu$ V) and current densities between 2 × 10<sup>3</sup> A m<sup>-2</sup> (1 mA) and 5 × 10<sup>8</sup> A m<sup>-2</sup> (250 A) were measured. The *n*-value tends to a constant value at low fields that is independent of temperature, but decreases at high compressive and tensile strains and low electric fields. In the high magnetic-field range, *n* is independent of *E*-field and can be approximated by a linear function of  $B - B_{c2}^*$  with a strain-independent gradient, where  $B_{c2}^*$  is an effective upper critical field.

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